

## $\beta$ -delayed proton decays and spin assignments for $^{140}\text{Tb}$ , $^{141}\text{Dy}$ and $^{143}\text{Dy}$

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Received: 1 January 2006 / Revised version: 24 April 2006 /

Published online: 29 May 2006 – © Società Italiana di Fisica / Springer-Verlag 2006

Communicated by D. Schwalm

**Abstract.** The proton-rich isotopes  $^{140}\text{Tb}$  and  $^{141}\text{Dy}$  were produced via the fusion evaporation reaction  $^{40}\text{Ca} + ^{106}\text{Cd}$ . Their  $\beta$ -delayed proton decays were studied by p- $\gamma$  coincidence in combination with a He-jet tape transport system, and half-lives, proton energy spectra,  $\gamma$ -transitions following the proton emission, as well as  $\beta$ -delayed proton branching ratios to the low-lying states in the grand-daughter nuclei were determined. Comparing the experimental data with statistical model calculations, the ground-state spins of  $^{140}\text{Tb}$  and  $^{141}\text{Dy}$  were found to be consistent with 7 and 9/2, respectively. The configuration-constrained nuclear potential energy surfaces (NPES) of  $^{140}\text{Tb}$  and  $^{141}\text{Dy}$  were calculated using the Woods-Saxon-Strutinsky method, which suggest the ground-state spins and parities of  $^{140}\text{Tb}$  and  $^{141}\text{Dy}$  to be  $7^+$  and  $9/2^-$ , respectively. In addition, the configuration-constrained NPES of  $^{143}\text{Dy}$  were calculated, which predict a  $1/2^+$  ground state and a  $11/2^-$  isomer with excitation energy of 198 keV. These findings are consistent with our previous experimental data on  $^{143}\text{Dy}$  reported in Eur. Phys. J. A **16**, 347 (2003).

**PACS.** 23.40.Hc Relation with nuclear matrix elements and nuclear structure – 21.10.Hw Spin, parity, and isobaric spin – 24.10.Pa Thermal and statistical models – 27.60.+j  $90 \leq A \leq 149$

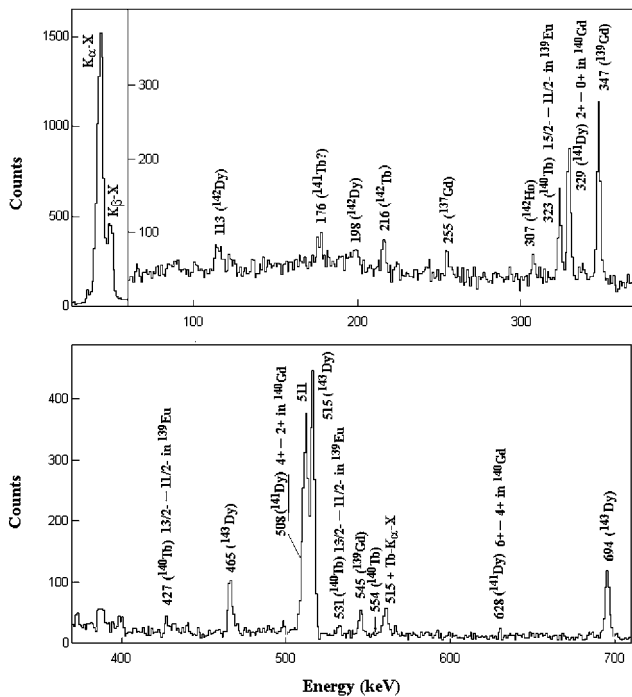
Wilmarth *et al.* [1] studied the  $\beta$ -delayed proton ( $\beta\text{p}$ ) decays of  $^{140}\text{Tb}$  and  $^{141}\text{Dy}$  near the proton drip line using the ISOL facility at LBL and reported the corresponding half-lives to be  $(2.4 \pm 0.5)$  s and  $(0.9 \pm 0.2)$  s, respectively. In addition,  $\gamma$ -rays of 329 and 508 keV were observed to follow the  $\beta\text{p}$  decay of  $^{141}\text{Dy}$ , which corresponds to the  $2^+ \rightarrow 0^+$  and  $4^+ \rightarrow 2^+$  transitions in the grand-daughter nucleus  $^{140}\text{Gd}$ . Later Gilat *et al.* [2] pointed out that the observed relative intensities of the 329 and 508 keV  $\gamma$ -rays observed in [1] are neither consistent with a  $1/2^+$  nor with a  $11/2^-$  assignment for the spin and parity of the precursor  $^{141}\text{Dy}$ . Instead, Gilat *et al.* suggested the spin and parity of  $^{141}\text{Dy}$  to be  $9/2^-$ , which was supported by their shell model calculation. The  $(\text{EC} + \beta^+)$  decay of  $^{140}\text{Tb}$  was first observed by Firestone [3] and the spin and parity of  $^{140}\text{Tb}$  was suggested to be  $5^+$ . Detailed data for the  $(\text{EC} + \beta^+)$  decay of  $^{140}\text{Tb}$  were reported by our group [4], including the  $(2.1 \pm 0.4)$  s half-life for  $^{140}\text{Tb}$  decay, and the spin and parity of  $^{140}\text{Tb}$  was suggested to be  $7^+$  instead of  $5^+$ . In the present work new studies on the  $\beta\text{p}$  decays of  $^{140}\text{Tb}$  and  $^{141}\text{Dy}$  are reported, and the final spin and parity assignments for  $^{140}\text{Tb}$  and  $^{141}\text{Dy}$  are proposed.

The experiment described here was carried out at the Sector-Focusing Cyclotron in the Institute of Modern Physics, Lanzhou, China. A schematic view of the experimental set-up is shown in fig. 1 of ref. [5]. A 232 MeV  $^{40}\text{Ca}^{12+}$  beam from the cyclotron entered a target chamber filled with 1 bar helium through a 1.89 mg/cm<sup>2</sup> thick Havar window. After traversing a 4.2 cm thick layer of helium gas and an aluminum degrader, the beam finally hits a  $^{106}\text{Cd}$  target (75% enriched) of about 1.8 mg/cm<sup>2</sup>. Four identical targets were mounted on a copper wheel surrounded by a cooling device, and the wheel was rotated by 90° once every 150 seconds. The beam energy in the middle of the target was 182 MeV, and the beam intensity was about 0.5 e $\mu$ A. The  $^{140}\text{Tb}$  and  $^{141}\text{Dy}$  were produced via the  $\alpha\text{n}$  (or  $2\text{p}3\text{n}$ ) and  $\alpha\text{pn}$  (or  $3\text{p}3\text{n}$ ) evaporation channels, respectively. We used a helium jet in combination with a tape transport system to periodically move the radioactivity into a shielded counting room, using  $\text{PbCl}_2$  at 430 °C as aerosol. The length of the capillary was about 6 m. The collection time, tape moving time, waiting time, and accumulation time were adjusted to 1.00, 0.16, 0.16, and 0.84 s, respectively. To study the  $\beta$ -delayed proton decays, proton-gamma coincidence measurements were carried out [6–8]. Two 570 mm<sup>2</sup>  $\times$  350  $\mu\text{m}$  totally depleted

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**Table 1.** Calculated and experimental relative branching ratios ( $b_{\beta p}$ ) to different final states in  $^{139}\text{Eu}$  from the  $\beta p$  decay of  $^{140}\text{Tb}$ , assuming different values for the initial spin and parity of  $^{140}\text{Tb}$ . The experimental relative  $b_{\beta p}$  leading to the  $15/2^-$  state was normalized to 30.

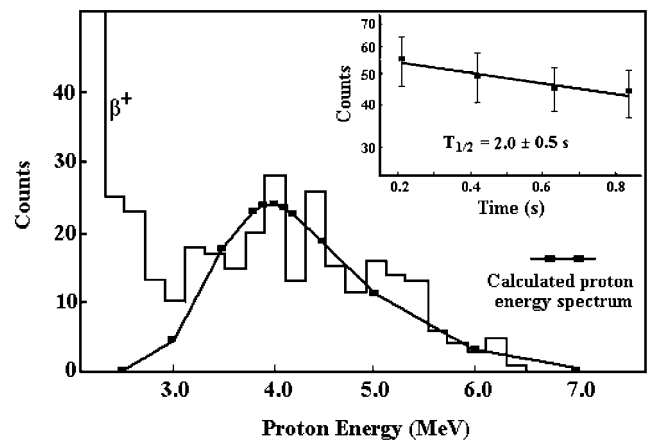
Initial spin and parity of $^{140}\text{Tb}$	Relative $b_{\beta p}$ to the final states				
	G.S.	323 keV	427 keV	531 keV	877 keV
	( $11/2^-$ )	( $15/2^-$ )	( $13/2_1^-$ )	( $13/2_2^-$ )	( $19/2^-$ )
$6^-$	66.9	13.0	12.1	7.9	0.1
$6^+$	63.3	14.2	13.4	8.8	0.2
$7^-$	46.5	27.8	15.1	9.7	0.9
$7^+$	45.6	29.5	14.6	9.6	0.7
$8^-$	28.9	44.4	13.4	8.7	4.5
$8^+$	24.7	43.6	15.6	10.3	5.7
Exp. value		$30 \pm 4$	$12 \pm 3$	$8.5 \pm 2$	$< 1$



**Fig. 1.** The measured  $\gamma$ (X)-ray spectrum in coincidence with delayed protons from 3.0 to 7.0 MeV observed in the reaction  $^{40}\text{Ca} + ^{106}\text{Cd}$ . The intense peaks are labeled by their energies in keV and their  $\beta p$  precursors.

silicon surface barrier detectors located on two opposite sides of the movable tape were used to detect the protons. Behind each silicon detector a coaxial HpGe(GMX) was placed to observe  $\gamma$ (X)-rays. Energy and time spectra of  $\gamma$ (X)-rays and protons were recorded in both single and coincidence modes.

The observed  $\gamma$ (X)-ray spectrum gated on  $\beta$ -delayed protons of 3.0–7.0 MeV is shown in fig. 1. The intense peaks, except 511 keV and X-rays, are labeled with their energies in keV and their  $\beta$ -delayed proton precursors. In particular, the 323, 427 and 531 keV  $\gamma$  lines were assigned to the  $15/2^- \rightarrow 11/2^-$  and to two different  $13/2^- \rightarrow 11/2^-$  transitions in the proton daughter nucleus  $^{139}\text{Eu}$  [9] following the  $\beta p$  decay of  $^{140}\text{Tb}$ , while the 329, 508 and

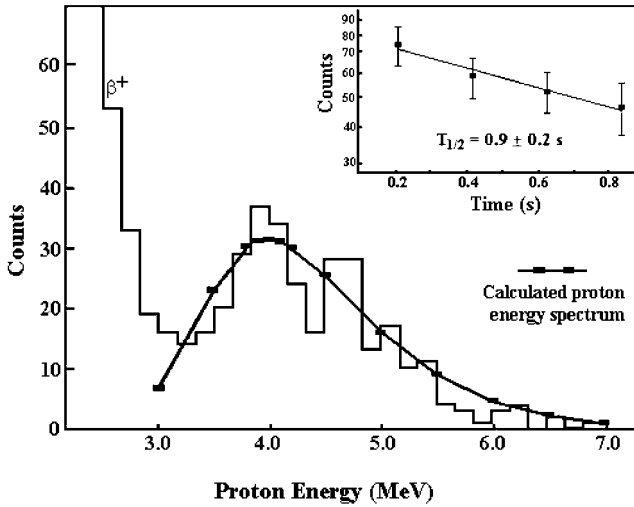


**Fig. 2.** The energy spectrum of  $\beta$ -delayed protons gated on the 323 keV  $\gamma$  line in  $^{139}\text{Eu}$  (histogram: experimental result; solid line: statistical-model calculations assuming an initial spin of 7 for the  $\beta p$  precursor  $^{140}\text{Tb}$ ). The insert displays the decay curve of the 323 keV  $\gamma$  line gated on the  $\beta$ -delayed protons.

628 keV  $\gamma$  lines were assigned to the  $2^+ \rightarrow 0^+$ ,  $4^+ \rightarrow 2^+$  and  $6^+ \rightarrow 4^+$  transitions in the proton daughter nucleus  $^{140}\text{Gd}$  [10] following the  $\beta p$  decay of  $^{141}\text{Dy}$ . We did not observe a  $\gamma$  line at an energy of 554 keV, which would correspond to the  $19/2^- \rightarrow 15/2^-$  transition in  $^{139}\text{Eu}$ .

The energy spectrum of  $\beta$ -delayed protons gated on the 323 keV  $\gamma$  line of  $^{139}\text{Eu}$  is shown in fig. 2, while the inset displays the decay curve of the 323 keV  $\gamma$  line when gated on the  $\beta$ -delayed protons. From the decay curve the half-life of  $^{140}\text{Tb}$  was extracted to be  $(2.0 \pm 0.5)$  s, which is consistent with the result given by Wilmarth *et al.* [1] as well as with our previous result reported in ref. [4].

The relative branching ratios ( $b_{\beta p}$ ) to different final states in the proton daughter nucleus  $^{139}\text{Eu}$  observed in the  $\beta p$  decay of  $^{140}\text{Tb}$  and the proton energy spectra were calculated for various values of the initial spin and parity of  $^{140}\text{Tb}$  using a statistical model [11], assuming a structureless Gamow-Teller (GT)  $\beta$ -strength function obtained from Gross theory [12]. The calculated  $b_{\beta p}$  are listed in table 1 together with the experimental values, which were determined by means of the relative intensities of the correspondent  $\gamma$  lines in fig. 1. Unfortunately, we could not



**Fig. 3.** The energy spectrum of  $\beta$ -delayed protons gated on the 329 keV  $\gamma$  line in  $^{140}\text{Gd}$  (histogram: experimental result; solid line: statistical-model calculations assuming an initial spin of  $9/2$  for the  $\beta p$  precursor  $^{141}\text{Dy}$ ). The insert displays the decay curve of the 329 keV  $\gamma$  line gated on the  $\beta$ -delayed protons.

**Table 2.** Calculated and experimental relative branching ratios ( $b_{\beta p}$ ) to different final states in  $^{140}\text{Gd}$  from the  $\beta p$  decay of  $^{141}\text{Dy}$ , assuming different values for the initial spin and parity of  $^{141}\text{Dy}$ . The experimental relative  $b_{\beta p}$  leading to the  $2^+$  state was normalized to 50.

Initial spin and parity of $^{141}\text{Dy}$	Relative $b_{\beta p}$ to the final states			
	G. S. ( $0^+$ )	329 keV ( $2^+$ )	836 keV ( $4^+$ )	1464 keV ( $6^+$ )
$7/2^-$	18.0	59.4	22.1	0.4
$7/2^+$	12.8	64.0	22.5	0.7
$9/2^-$	4.9	49.2	41.1	4.8
$9/2^+$	9.5	48.6	38.8	3.1
$11/2^-$	3.9	32.3	50.1	13.6
$11/2^+$	1.2	29.3	55.3	14.3
Exp. value		$50 \pm 6$	$39 \pm 8$	$7 \pm 4$

obtain the experimental  $b_{\beta p}$  to the ground state in  $^{139}\text{Eu}$  because of the restriction of the p- $\gamma$  coincidence method. Comparing the calculated branching ratios with the experimental values, the closest agreement is found when assuming the ground-state spin and parity of  $^{140}\text{Tb}$  to be  $7^+$  or  $7^-$ . Moreover, the proton energy spectrum is reproduced reasonably well if  $^{140}\text{Tb}$  is assumed to have  $7^+$  or  $7^-$  (see fig. 2), the difference of the calculated energy spectra between the two parities being too small to be seen in fig. 2.

The energy spectrum of  $\beta$ -delayed protons gated on the 329 keV  $\gamma$  line of  $^{140}\text{Gd}$  is shown in fig. 3, while the inset displays the decay curve of the 329 keV  $\gamma$  line when gated on the  $\beta$ -delayed protons. From the decay curve the half-life of  $^{141}\text{Dy}$  was extracted to be  $(0.9 \pm 0.2)$  s, which is consistent with the result given by Wilmarth *et al.* [1].

The relative  $b_{\beta p}$  to different final states in the proton daughter nucleus  $^{140}\text{Gd}$  observed in the  $\beta$ -delayed proton decay of  $^{141}\text{Dy}$  and the proton energy spectra were also

calculated for various values of the initial spin and parity of  $^{140}\text{Tb}$  using the statistical model [11]. The calculated  $b_{\beta p}$  are given in table 2 together with the experimental values. Comparing the calculated branching ratios with the experimental values, the closest agreement is found when assuming the ground-state spin and parity of  $^{141}\text{Dy}$  to be  $9/2^+$  or  $9/2^-$ . Moreover, the proton energy spectrum is reproduced reasonably well if  $^{141}\text{Dy}$  is assumed to have  $9/2^+$  or  $9/2^-$  (see fig. 3), the difference of the calculated energy spectra between the two parities being too small to be seen in fig. 3.

To shed more light on the ground-state properties of  $^{140}\text{Tb}$  and  $^{141}\text{Dy}$ , the configuration-constrained NPES were calculated using the Woods-Saxon-Strutinsky method [13]. For  $^{140}\text{Tb}$  a minimum at deformation parameters  $\beta_2 = 0.243$  and  $\gamma = 22.5^\circ$  was found, which corresponds to the configuration  $(\pi 5/2^- [532] \times \nu 9/2^- [514]) 7^+$ , while for  $^{141}\text{Dy}$  a minimum at  $\beta_2 = 0.242$  and  $\gamma = 21.5^\circ$  was observed corresponding to the configuration  $(\nu 9/2^- [514]) 9/2^-$ . These findings are not only in good agreement with the experimental results related to  $\beta p$  decay, but also with the spin assignments for  $^{141}\text{Dy}$  given by Gilat *et al.* [2] and for  $^{140}\text{Tb}$  as deduced in our previous study of the  $(\text{EC} + \beta^+)$  decay of  $^{140}\text{Tb}$  [4]. We, therefore, assign  $7^+$  and  $9/2^-$  to the ground state of  $^{140}\text{Tb}$  and  $^{141}\text{Dy}$ , respectively.

The ground-state spin and parity of  $^{143}\text{Dy}$  was proposed as  $1/2^+$  by Audi *et al.* [14] based on systematics and later supported by an in-beam  $\gamma$  study [15]. Moreover, the existence of an  $11/2^-$  isomer with the energy of 310.7 keV was conjectured from these in-beam  $\gamma$  studies. Later, the decay of  $^{143}\text{Dy}$  was observed and  $(\text{EC} + \beta^+)$  as well as  $\beta p$  decay schemes for the  $1/2^+$  ground state and the  $11/2^-$  isomer of  $^{143}\text{Dy}$  were proposed by us in ref. [5]. Calculating the configuration-constrained NPES also for  $^{143}\text{Dy}$ , a minimum at  $\beta_2 = 0.202$  and  $\gamma = 26^\circ$  was obtained, which corresponds to the configuration of  $\nu 1/2^+ [400]$ . In addition, a second minimum at  $\beta_2 = 0.198$  and  $\gamma = 47^\circ$  was found, which corresponds to the spin assignment of  $11/2^-$ . Thus the NPES do support also our previous experimental results obtained for  $^{143}\text{Dy}$ .

This work was supported by the National Natural Science Foundation of China (10375078 and 10475002).

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